

Interaction of hydrogen atoms with carbon- sp^2 structures

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Outline

- 1 Introduction
- 2 Adsorption energetics
 - ‘Bulk’ adsorption and clustering
 - Edge effects
- 3 Eley-Rideal reaction
 - Dynamics at cold E_{coll}



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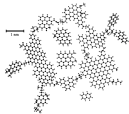
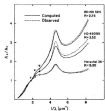
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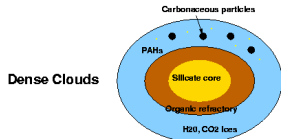
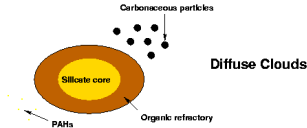
H₂ in the ISM

- Hydrogen is the most abundant element of the Universe
- H₂ is formed on the surface of *dust grain*



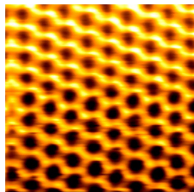
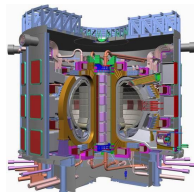
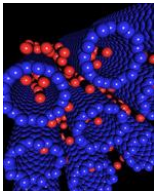
Hydrogen-graphite is an important model for understanding H₂ formation in ISM

$f_{\text{grain}} = n_{\text{grain}}/n_{\text{H}} \sim 10^{-12}$ i.e. $\sim 1\%$ of ISM mass



Technology

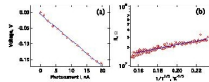
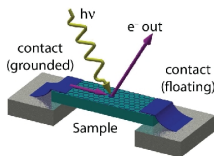
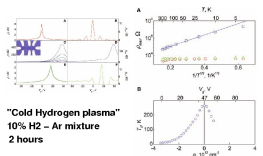
- Hydrogen storage
- Nuclear fusion
- Nanoelectronics, spintronics, nanomagnetism



Technology: graphene physics and devices

Graphene is a true **2D-electron gas** (2DEG) system with pseudo-relativistic charge-carriers

MIT occurs when **hydrogenating** graphene



UHV ($p \sim 10^{-9}$ Torr)
 $T(\text{H}_2) \sim 2000$ C

.. σ vs T agrees well with VRH in two dimensions

High n_H : D. C. Elias *et al.*, *Science* **323**, 610 (2009)

Low n_H : A. Bostwick *et al.*, *Phys. Rev. Lett.* **103**, 056404 (2009)

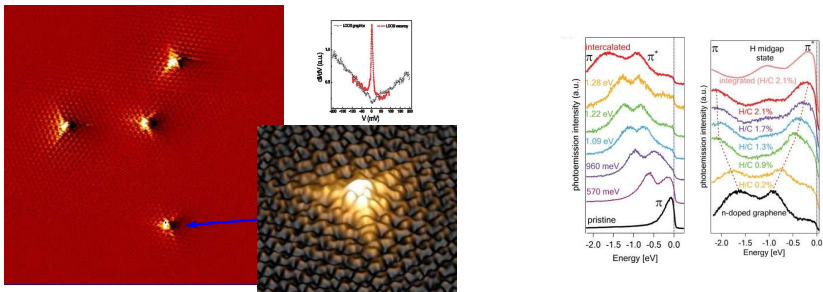


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Midgap states



M.M. Ugeda, I. Brihuega, F. Guinea and J.M. Gomez-Rodriguez, *Phys. Rev. Lett.* **104**, 096804 (2010)

D. Haberer *et al.*, *Phys. Rev. B* **83**, 165433 (2011)

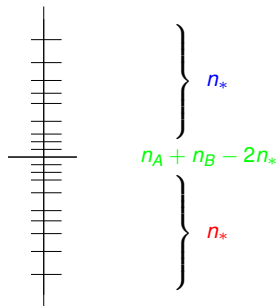


Midgap states

$$H^\pi \approx \sum_{\tau, ij} (t_{ij} a_{i,\tau}^\dagger b_{j,\tau} + t_{ji} b_{j,\tau}^\dagger a_{i,\tau}) + U \sum_i n_{i,\tau} n_{i,-\tau}$$

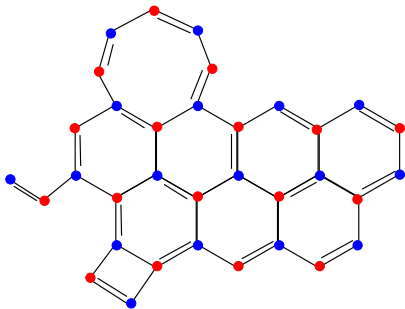
Basic results

- **Electron-hole** symmetry: $\epsilon_i \rightarrow -\epsilon_i$
- **Imbalance** rule: $\nu \geq \eta = |n_A - n_B|$
- **Spin** alignment: $S = |n_A - n_B|/2$



Midgap states

$$H^\pi \approx \sum_{\sigma,ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma})$$



Electron-hole symmetry

$$b_i \rightarrow -b_i \implies H^\pi \rightarrow -H^\pi$$

$$\epsilon_i, |\psi_i^{(+)}\rangle = \sum_k \alpha_k |a_k\rangle + \sum_j \beta_j |b_j\rangle$$

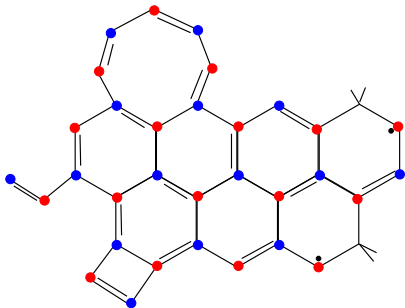
↓

$$-\epsilon_i, |\psi_i^{(-)}\rangle = \sum_k \alpha_k |a_k\rangle - \sum_j \beta_j |b_j\rangle$$



Midgap states

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma})$$



Imbalance rule

Let $n_A > n_B$, $\mathbf{T}(n_B \times n_A)$

$$\begin{bmatrix} \mathbf{0} & \mathbf{T}^\dagger \\ \mathbf{T} & \mathbf{0} \end{bmatrix} \begin{bmatrix} \alpha \\ \beta \end{bmatrix} = \begin{bmatrix} \mathbf{0} \\ \mathbf{0} \end{bmatrix}$$

$\Rightarrow \mathbf{T}\alpha = \mathbf{0}$ has (at least)

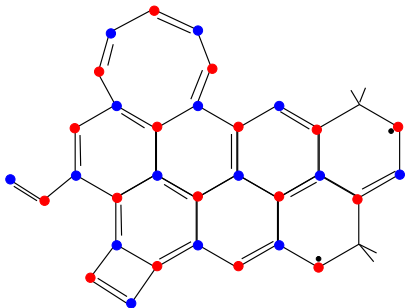
$n_A - n_B$ solutions

$\Rightarrow \psi_{E=0}$ have vanishing components on B sites



Midgap states

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} a_{i, \sigma}^\dagger b_{j, \sigma} + t_{ji} b_{j, \sigma}^\dagger a_{i, \sigma}) + U \sum_i n_{i, \uparrow} n_{i, \downarrow}$$



Spin alignment

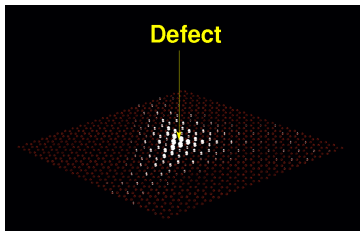
If $U > 0$, the ground-state at *half-filling* has

$$S = |n_A - n_B|/2 = n_I/2$$

E.H. Lieb, *Phys. Rev. Lett.* **62**, 1201 (1989)

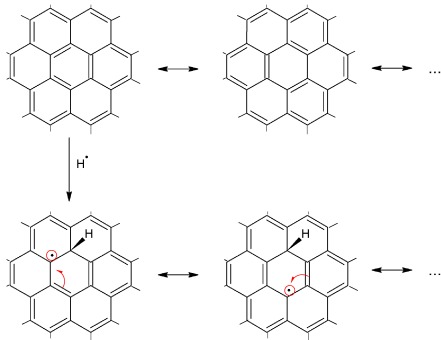


Midgap states



$$\psi(x, y, z) \sim 1/r$$

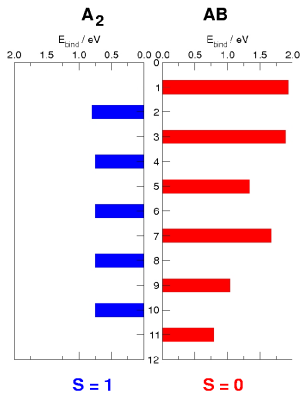
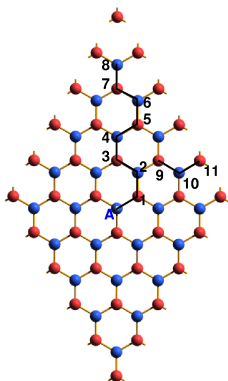
V. M. Pereira *et al.*, *Phys. Rev. Lett.* **96**, 036801 (2006);
Phys. Rev. B **77**, 115109 (2008)



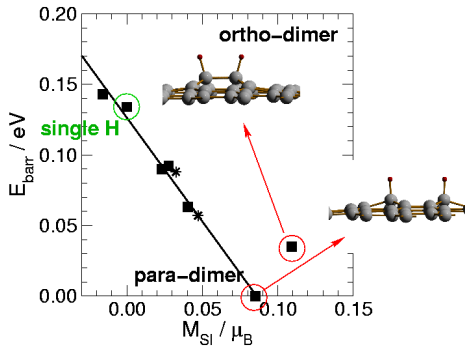
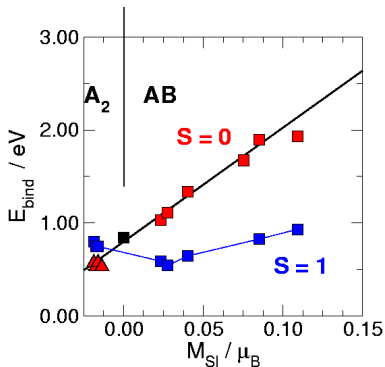
See also, e.g., Y. Ferro *et al.*, *Phys. Rev. B* **78**, 085417 (2008)



Dimers



Dimers

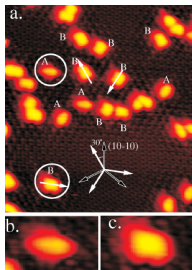


S. Casolo, O.M. Lovvik, R. Martinazzo and G.F. Tantardini, *J. Chem. Phys.* **130** 054704 (2009)
arXiv:0808.1312 (2008)

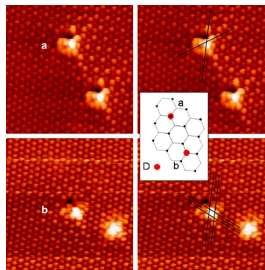
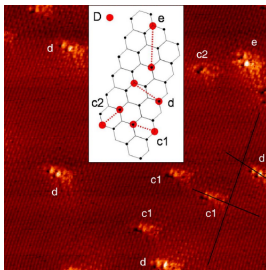
Preferential sticking: L. Hornekaer *et al.*, *Phys. Rev. Lett.* **96** 156104 (2006)



Dimers



[1]



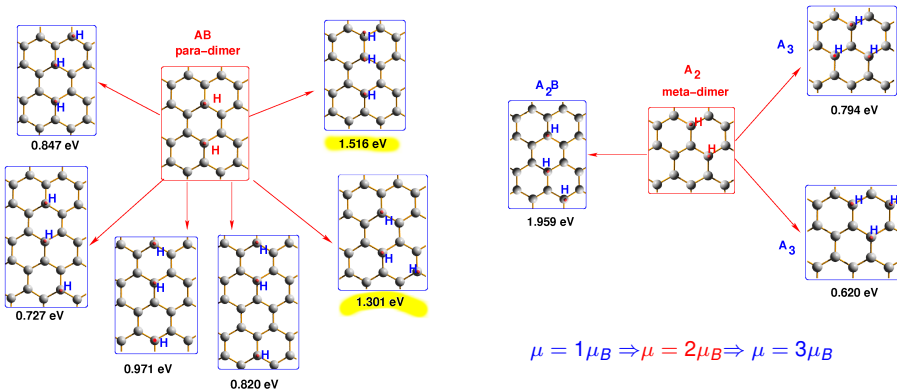
[2]

[1] L. Hornekaer, Z. Slijvančanin, W. Xu, R. Otero, E. Rauls, I. Stensgaard, E. Laegsgaard, B. Hammer and F. Besenbacher. *Phys. Rev. Lett.* **96** 156104 (2006)

[2] A. Andree, M. Le Lay, T. Zecho and J. Kupper, *Chem. Phys. Lett.* **425** 99 (2006)



3-atom clusters



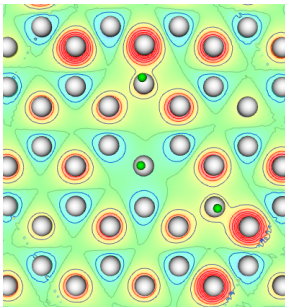
$$\mu = 1\mu_B \Rightarrow \mu = 2\mu_B \Rightarrow \mu = 3\mu_B$$

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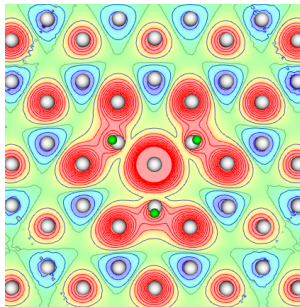


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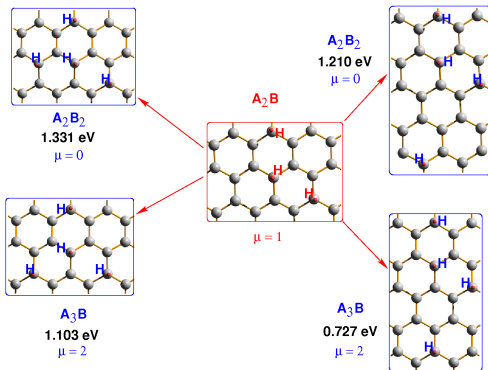
A_2B



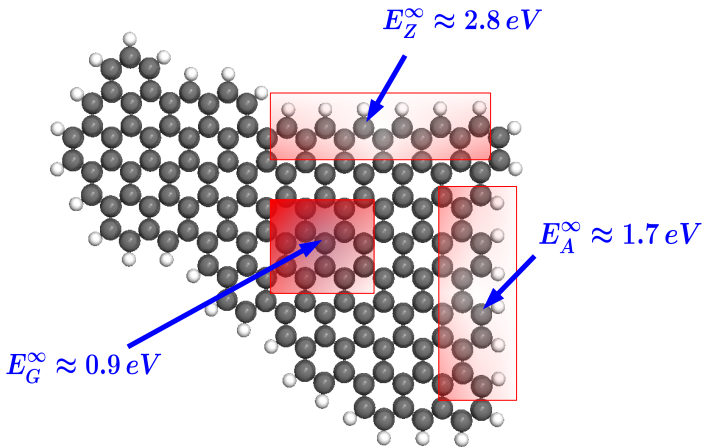
A_3



4-atom clusters



Role of edges



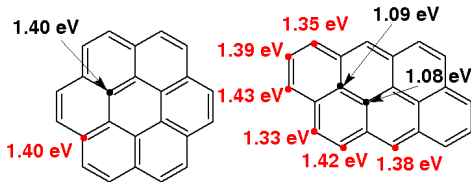
'Geometric' effect?

'Reorganization' energy upon binding

$$\delta E = E(\text{PAH}^*) - E(\text{PAH}^{\text{eq}})$$

E sites: $\delta E \sim 1.4 \pm 0.1 \text{ eV}$

G sites: $\delta E \sim 1.0 \pm 0.1 \text{ eV}$



...purely **electronic** effect



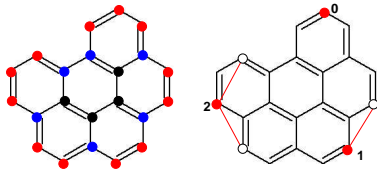
Hints from the tight-binding Hamiltonian H^π

Shape of low-energy orbitals
..from a 'lattice renormalization'

- Coordination (Z)
- Hypercoordination (ξ)
- sublattice imbalance (η)

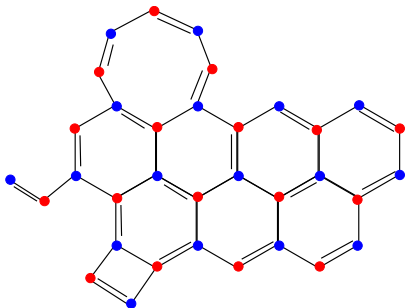
$$Z = 2 \Rightarrow \mathbf{E}$$

$$Z = 3 \Rightarrow \mathbf{F, G}$$



Hints from the tight-binding Hamiltonian H^π

$$H^\pi \approx \sum_{\sigma, ij} (t_{ij} a_{i,\sigma}^\dagger b_{j,\sigma} + t_{ji} b_{j,\sigma}^\dagger a_{i,\sigma})$$



'Lattice renormalization'

$$\tilde{H}_{AA} = H_{AB} H_{BA}$$

$$\tilde{\epsilon}_i, |\psi_{A,i}\rangle$$

$$\Downarrow$$

$$\begin{aligned} \epsilon_i^\pm &= \pm \sqrt{\tilde{\epsilon}_i}, |\psi_i^{(\pm)}\rangle = |\psi_{A,i}\rangle \pm |\psi_{B,i}\rangle \\ |\psi_{B,i}\rangle &= \tilde{\epsilon}_i^{-1/2} H_{BA} |\psi_{A,i}\rangle \end{aligned}$$

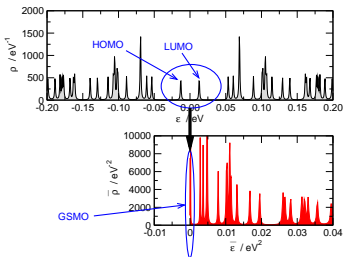
G. Naumis, *Phys. Rev. B* **76** 153403 (2007)

R. Martinazzo, S. Casolo and G.F. Tantardini, *Phys. Rev. B* **81** 245420 (2010)



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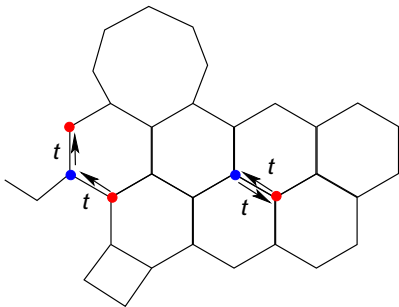
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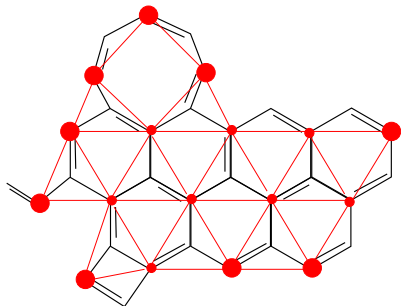
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Hints from the tight-binding Hamiltonian H^π

$$\tilde{H}^\pi \approx \sum_i Z_i t^2 a_i^\dagger a_i + \sum_{ij} t^2 a_i^\dagger a_j$$



'Lattice renormalization'

$$\tilde{H}_{AA} = H_{AB} H_{BA}$$

$$\tilde{\epsilon}_i, |\psi_{A,i}\rangle$$

$$\Downarrow$$

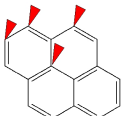
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G. Naumis, *Phys. Rev. B* **76** 153403 (2007)

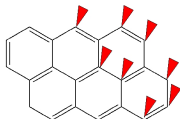
R. Martinazzo, S. Casolo and G.F. Tantardini, *Phys. Rev. B* **81** 245420 (2010)



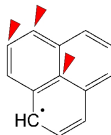
Systems



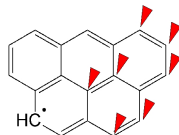
pirene



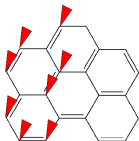
dibenzo[def,mno]crisene /
antrantrene



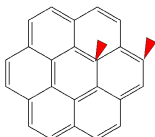
perinaftene / fenalene



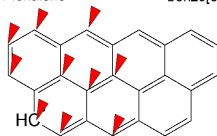
benzo[cd]pirenile



benzo[ghi]perilene



coronene



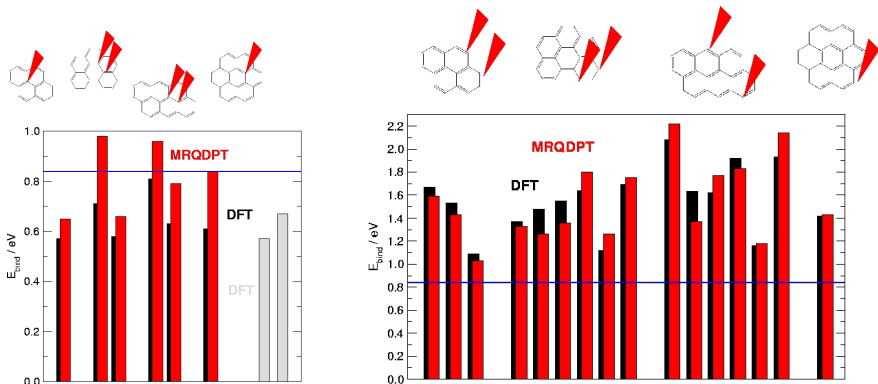
7 - PAH

$$\eta = 0$$

$$\eta \neq 0$$



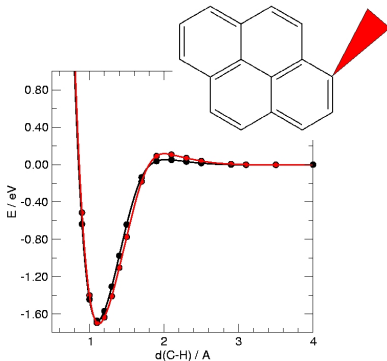
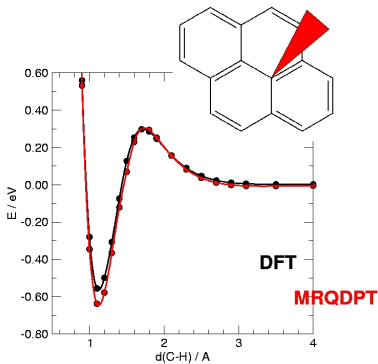
Graphitic vs edge carbons



M. Bonfanti, S. Casolo, G. F. Tantardini, A. Ponti and R. Martinazzo, *JCP*, in press; arXiv:1107.4324 (2011)



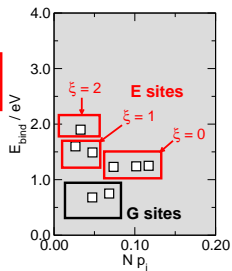
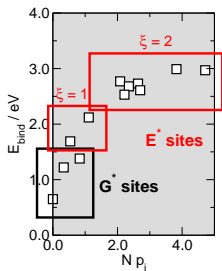
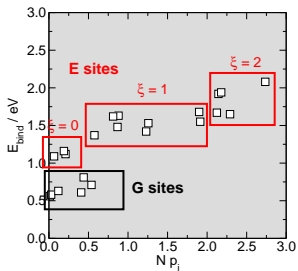
Adsorption paths



M. Bonfanti, S. Casolo, G. F. Tantardini, A. Ponti and R. Martinazzo, *JCP*, in press; arXiv:1107.4324 (2011)



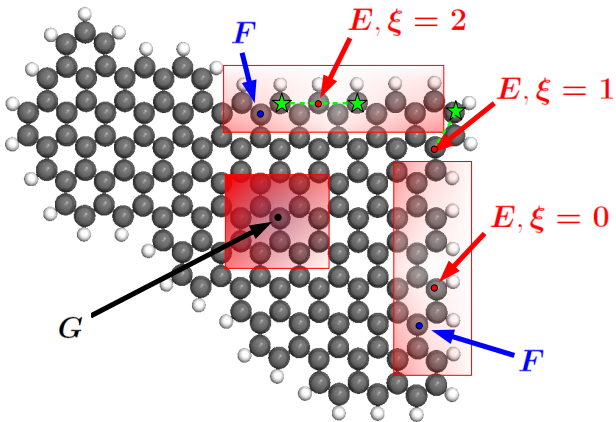
Predicting reactivity

 $\eta = 0$ $\eta \neq 0$ 

M. Bonfanti, S. Casolo, G. F. Tantardini, A. Ponti and R. Martinazzo, *JCP*, in press; arXiv:1107.4324 (2011)



Predicting reactivity



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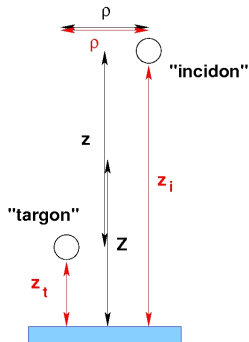


Reaction: technicalities

- **Rigid, flat** surface approximation¹
- **Split-Operator** with FFT along cartesian coordinates and DBT along ρ ¹
- propagation in both **product** and **reagent** coordinate sets²

⇒ state-to-state, energy-resolved cross sections for **all** possible processes

- [1] M. Persson and B. Jackson, J. Chem. Phys. 102, 1078 (1995); D. Lemoine and B. Jackson, Comput. Phys. Commun. 137, 415 (2001)
[2] R. Martinazzo and G.F. Tantardini, J. Phys. Chem. A, 109 (2005) 9379; J. Chem. Phys. 124, 124703 (2006); J. Chem. Phys. 124, 124704 (2006)



Reaction: technicalities (low E_{col})

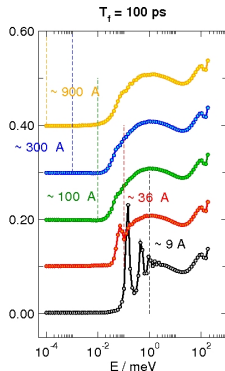
- Two-wavepacket approach¹
- Transmission-free² absorbing potentials and Fourier mapping³ in reagent coordinates

In 3D $T_f=25-30$ ps and AP lengths $\sim 50\text{\AA}$ in order to get converged xsections down to $\sim 10^{-5}$ eV, i.e. ~ 0.1 K

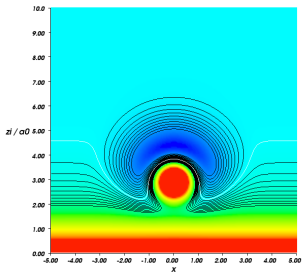
[1] R. Martinazzo and G.F. Tantardini, J. Chem. Phys. 122, 094109 (2005)

[2] D. Manolopoulos, J. Chem. Phys. 117, 9552 (2002)

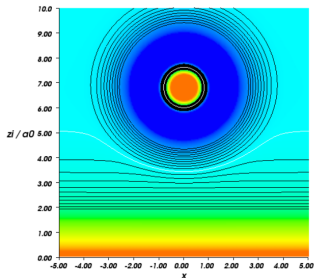
[3] A.G. Borisov, J. Chem. Phys. 114, 7770 (2001)



Reaction: Potential Energy Surfaces



Chemisorbed target H (z_{eq})

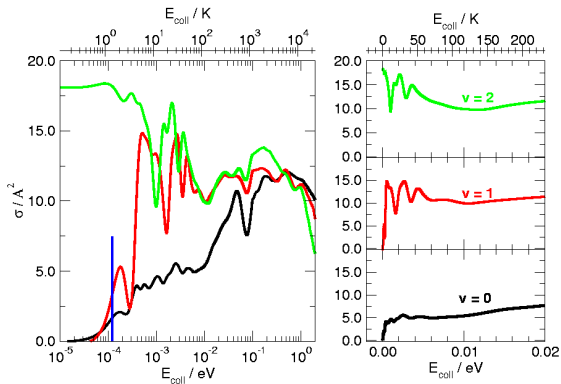


Physisorbed target H (z_{eq})

X. Sha, B. Jackson and D. Lemoine, J. Chem. Phys. 116, 7158 (2002)



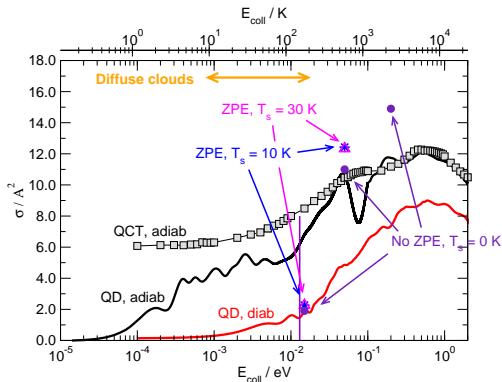
I. H-chemisorbed case



S. Casolo, M. Bonfanti, R. Martinazzo and G.F. Tantardini, *J. Phys. Chem. A*, **113** 14545 (2009)



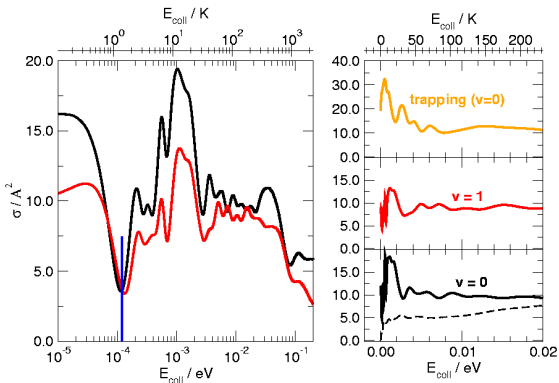
I. H-chemisorbed case

QCT comparison, $\nu = 0$ 

M. Sizun, D. Bachellerie, F. Anguillon, V. Sidis *Chem. Phys. Lett.* 32 498 2010
 D. Bachellerie, M. Sizun, F. Anguillon, D. Teillet-Billy, N. Rougeau, *Phys. Chem. Chem. Phys.* 2715 11 2009



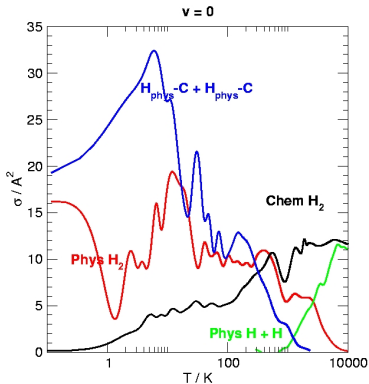
II. H-physisorbed case



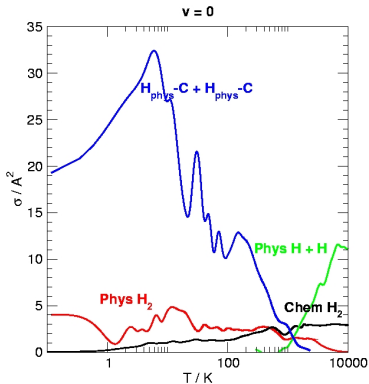
S. Casolo, M. Bonfanti, R. Martinazzo and G.F. Tantardini, *J. Phys. Chem. A*, **113** 14545 (2009)



H-chem vs H-phys



H-chem vs H-phys



Cross-sections have to be corrected for the **spin** statistics (1/4)



Summary

- Thermodynamically and kinetically favoured H clusters in the bulk **minimize** sublattice imbalance
- Edges are chemically **active**, adsorption may be **barrierless**
- At low energies, **physisorbed** H atoms are more reactive than **chemisorbed** species



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Notur
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Chemical Dynamics Theory Group

<http://users.unimi.it/cdtg>

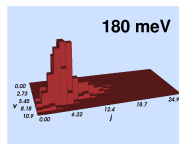
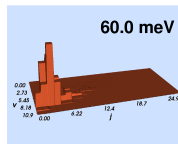
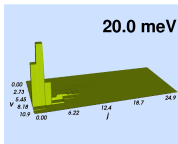
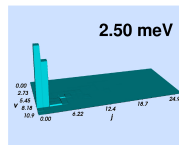
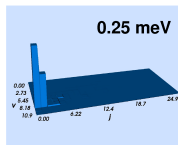
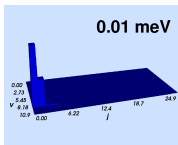
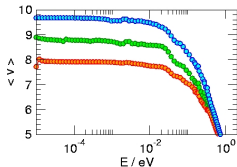
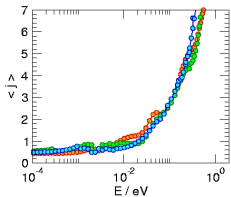


Acknowledgements

Thank you for your attention!



I. H-chemisorbed case



I. H-chemisorbed case

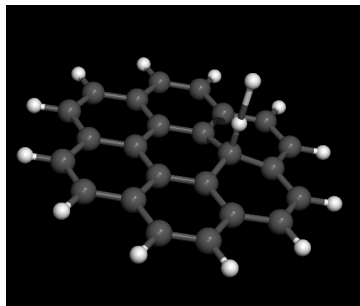
Challenges

- **Quantum** dynamics is needed at ISM conditions
- C_{puck} atom plays an **active** role in the dynamics
- **Energy transfer** might be important
- **Accurate** Potential Energy Surfaces

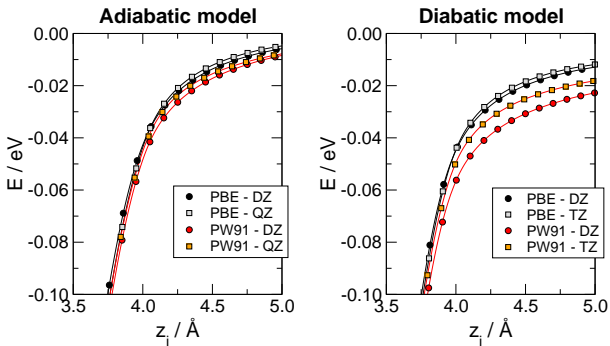


Checking the models

- **Coronene** and 2x2, 3x3 **periodic** models
- **Diabatic** and **Adiabatic** cases
- **PBE** (PW91)
- **cc-pVDZ**, (cc-pVTZ, cc-pvQZ) / 15x15x1, $E_{cut}=500$ eV



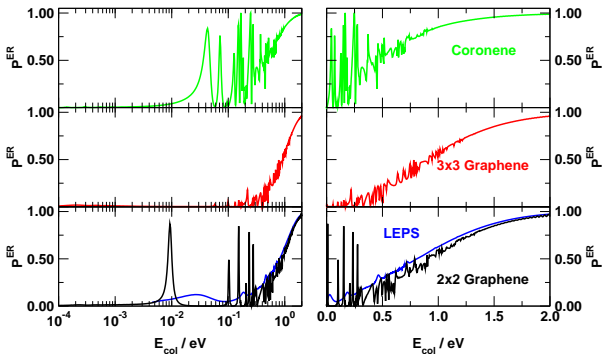
Energy barrier?



M. Bonfanti, S. Casolo, G. F. Tantardini and R. Martinazzo, *Phys. Chem. Chem. Phys.*, **13** 16680 (2011)



Influence on the (collinear) dynamics



M. Bonfanti, S. Casolo, G. F. Tantardini and R. Martinazzo, *Phys. Chem. Chem. Phys.*, **13** 16680 (2011)

